



Deutsches Elektronen-Synchrotron **DESY**  
Ein Forschungszentrum  
der Helmholtz-Gemeinschaft



EBERHARD KARLS  
**UNIVERSITÄT**  
**TÜBINGEN**



# CLOSED-LOOP EXPERIMENTS USING ML-BASED ONLINE ANALYSIS AT SYNCHROTRON BEAMLINES: A CASE STUDY IN X-RAY REFLECTOMETRY

Linus Pithan, Vladimir Starostin, Valentin Munteanu,  
Alexander Hinderhofer, Stefan Kowarik, Frank Schreiber

# Agenda – It's about ML and Reflectometry

A story of an excellent, long-standing collaboration



2019 – first work on ML in reflectometry

2022 – MLreflect package

2023 – closed loop experiment

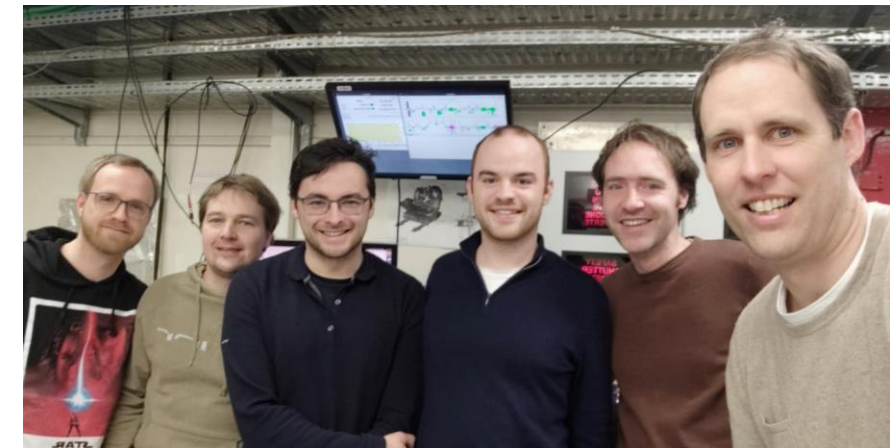
2023 - discretization-invariant learning / Neural operators

2024 – prior-informed regression. Reflectorch package

2024 – normalizing flows / probabilistic SLD reconstruction



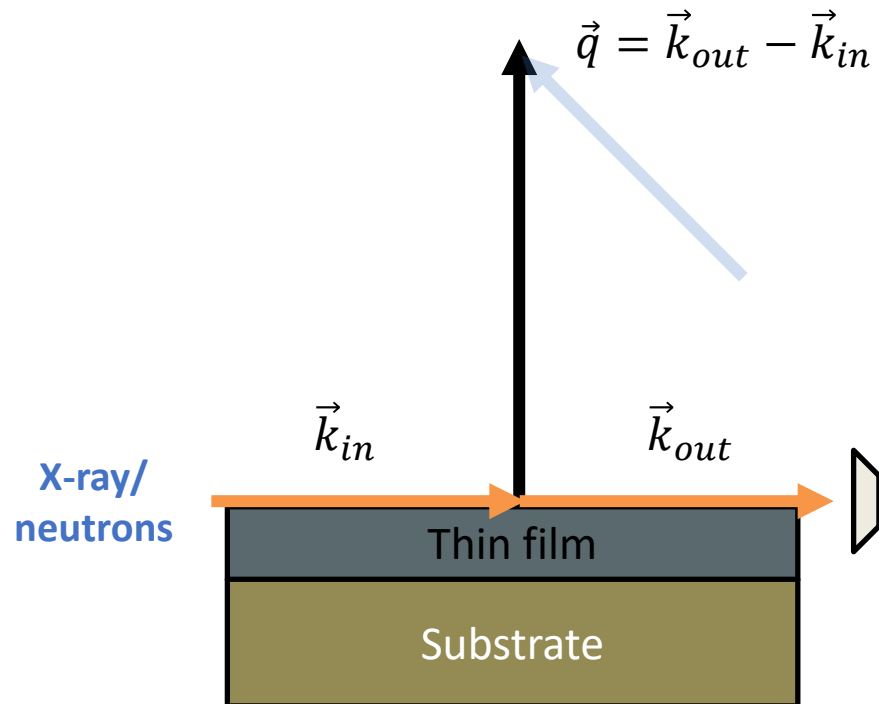
Frank Schreiber's group (Uni Tübingen)  
Stefan Kowarik's group (Uni Graz)  
Vladimir Starostin (ML Cluster Tübingen)



# X-ray and neutron reflectivity (XRR/NR)

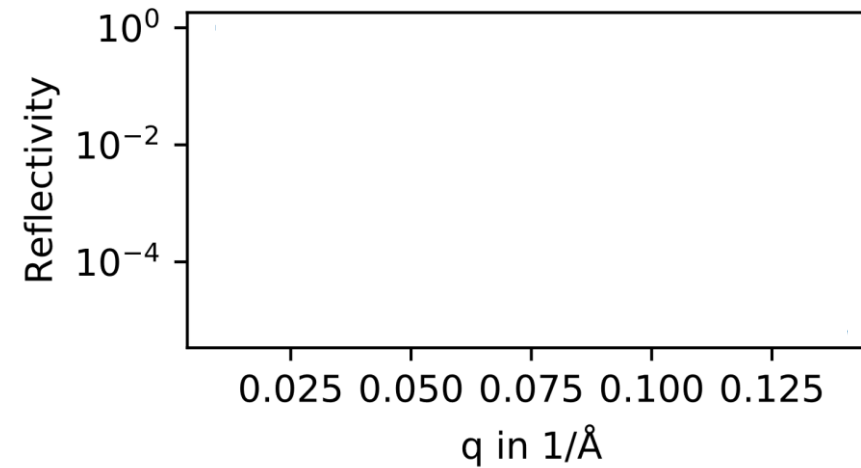
## Experiment

X-ray beam at certain discrete angles



## Data

Reflected beam intensity for each angle



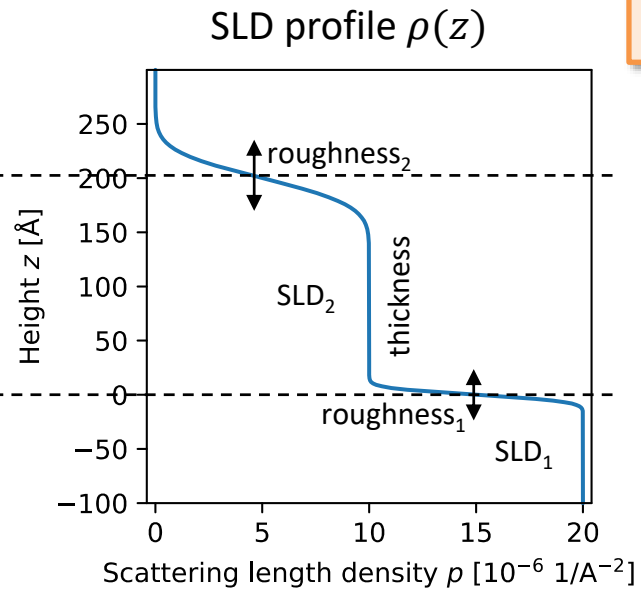
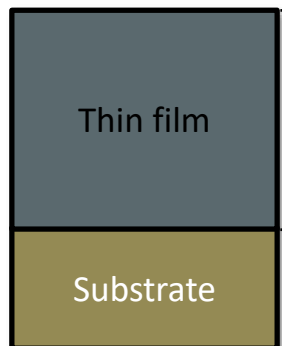
Shape of reflectivity curve provides information about thin film properties

# ML: Modeling of the “back-transformation”



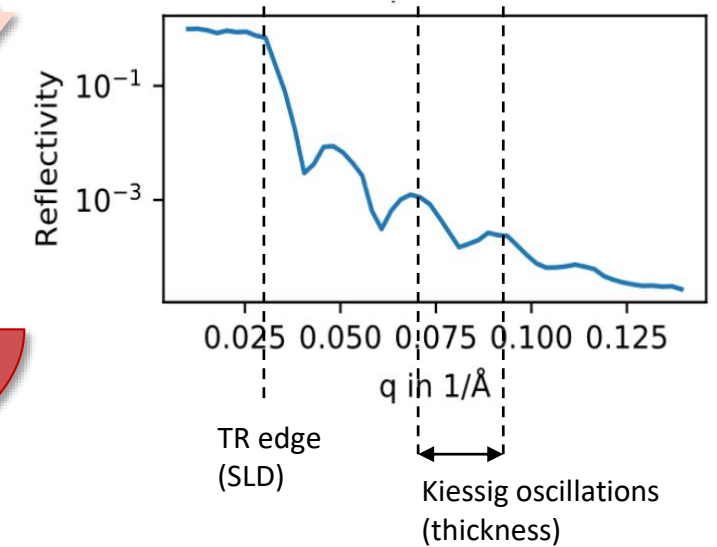
$$R(q_z) \propto q_z^{-4} \left| \int \frac{d\rho(z)}{dz} e^{iq_z z} dz \right|^2$$

Fourier transform with phase loss!



Theoretical models  
(Parratt, matrix method,  
kinematic approximation)

Measured reflectivity curves  $R(q; \mathbf{p})$



Iterative fitting  
(LMS,  $\chi^2$ , posterior  
probability estimation)

No analytical  
“back-transformation”!

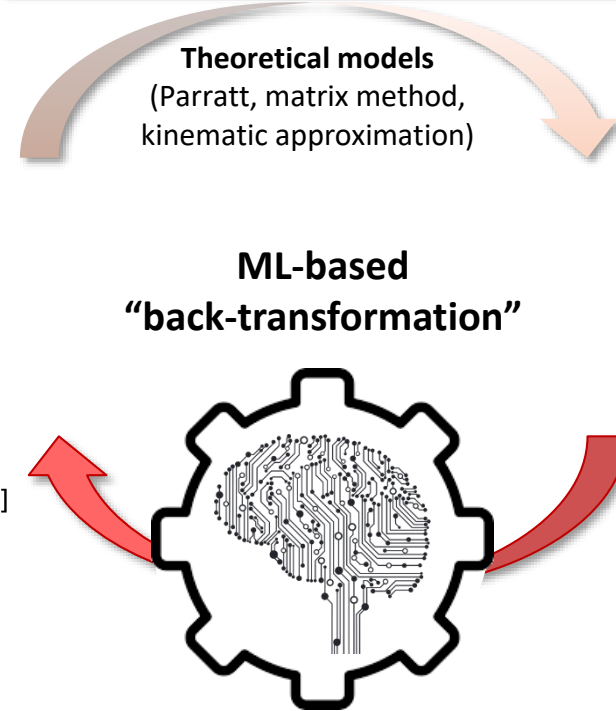
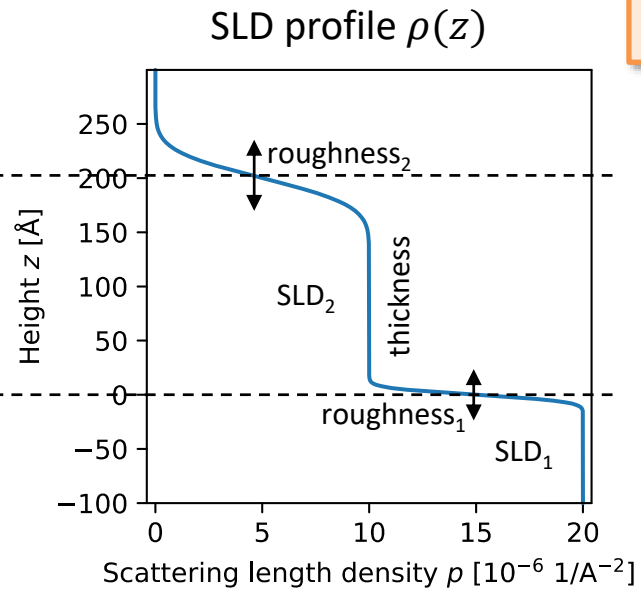
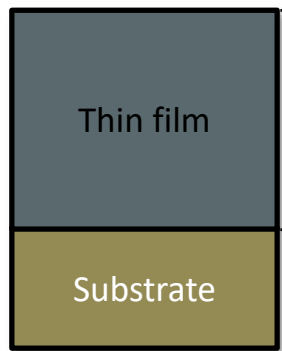
SLD profile usually parameterized, *i.e.*  
 $\rho(z) = \rho(z; \mathbf{p})$ , with  $\mathbf{p} = (\text{thickness, roughness, SLD})$

# ML: Modeling of the “back-transformation”

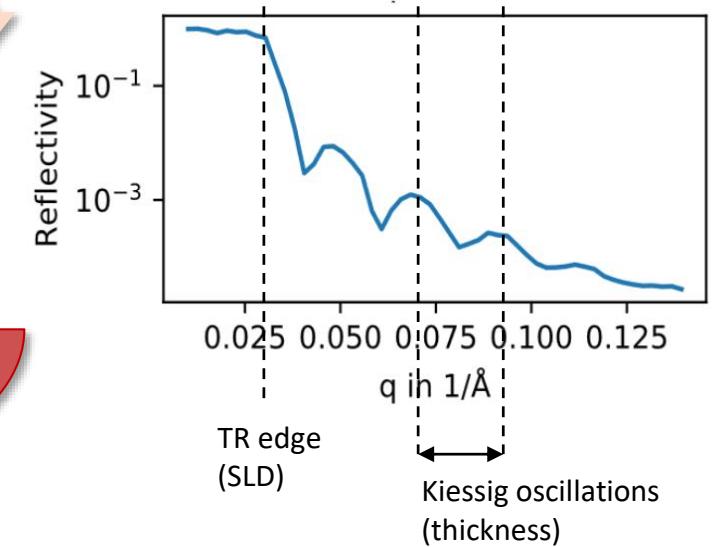


$$R(q_z) \propto q_z^{-4} \left| \int \frac{d\rho(z)}{dz} e^{iq_z z} dz \right|^2$$

Fourier transform with phase loss!



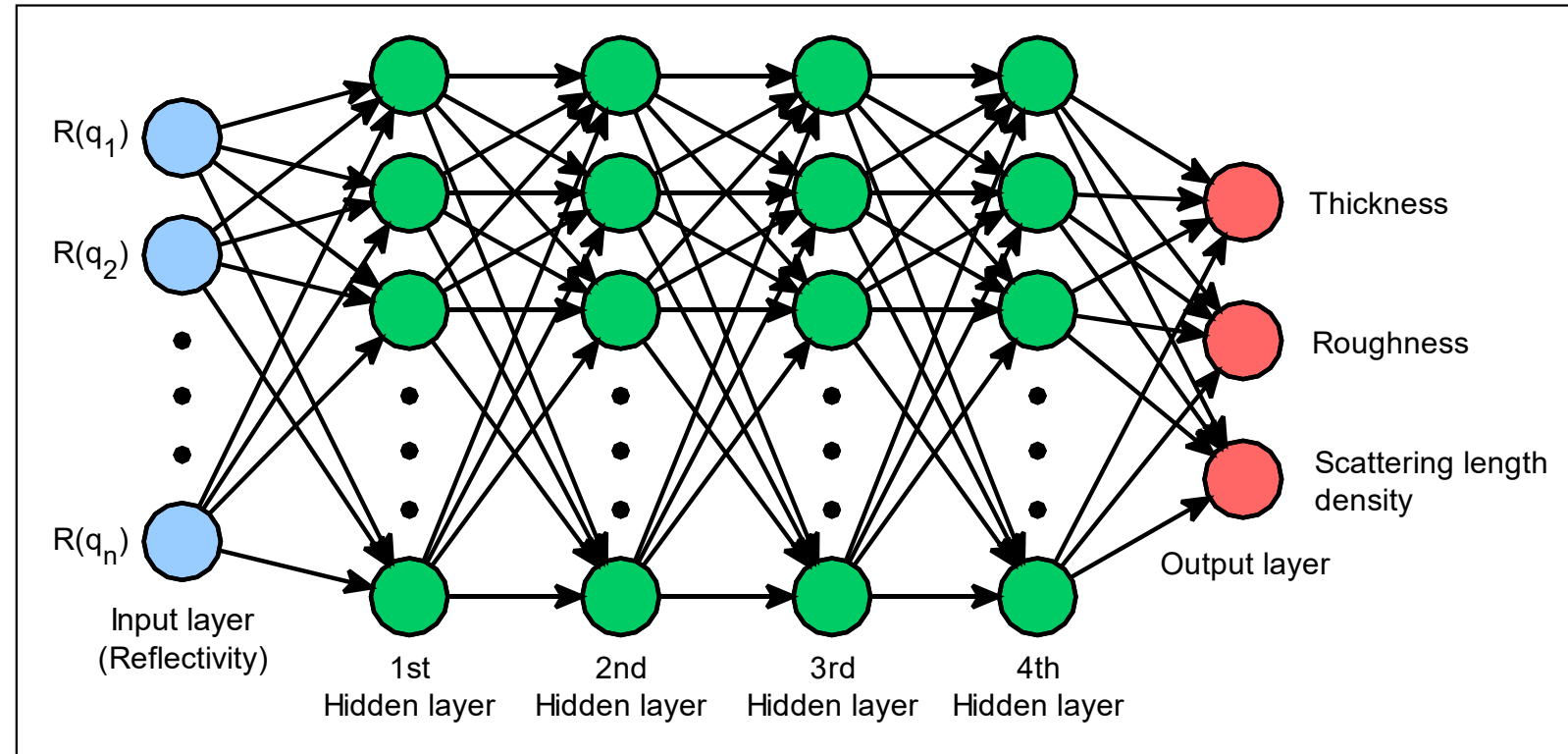
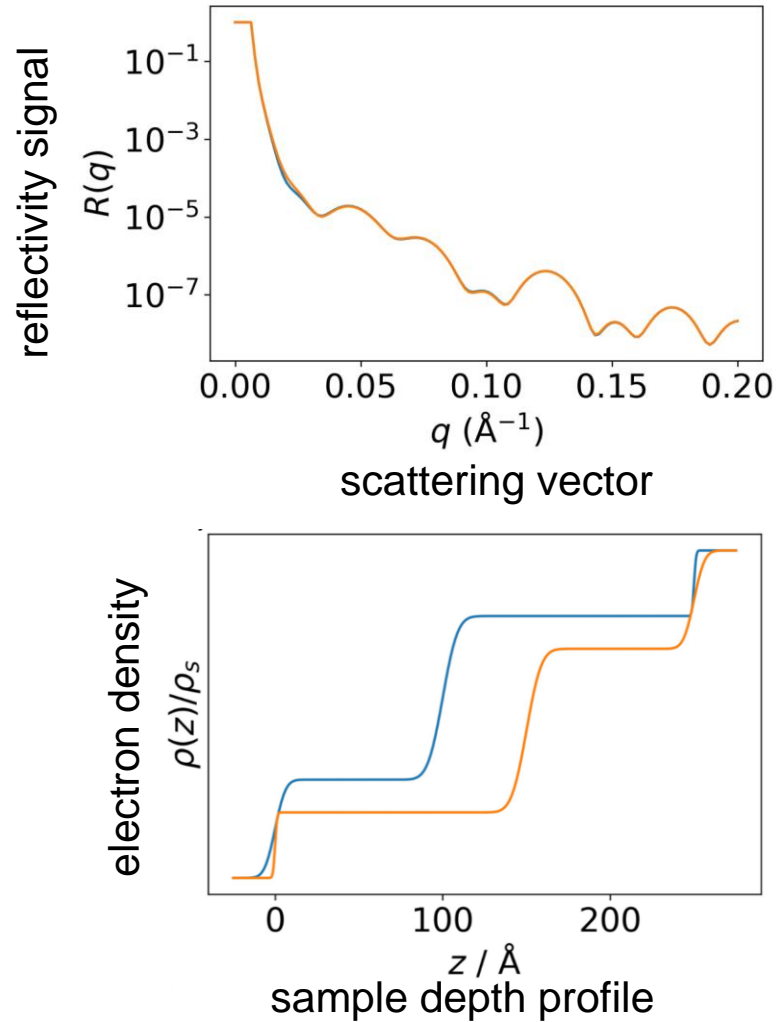
Measured reflectivity curves  $R(q; p)$



SLD profile usually parameterized, *i.e.*  
 $\rho(z) = \rho(z; \mathbf{p})$ , with  $\mathbf{p} = (\text{thickness, roughness, SLD})$



# ill-posed inverse problems



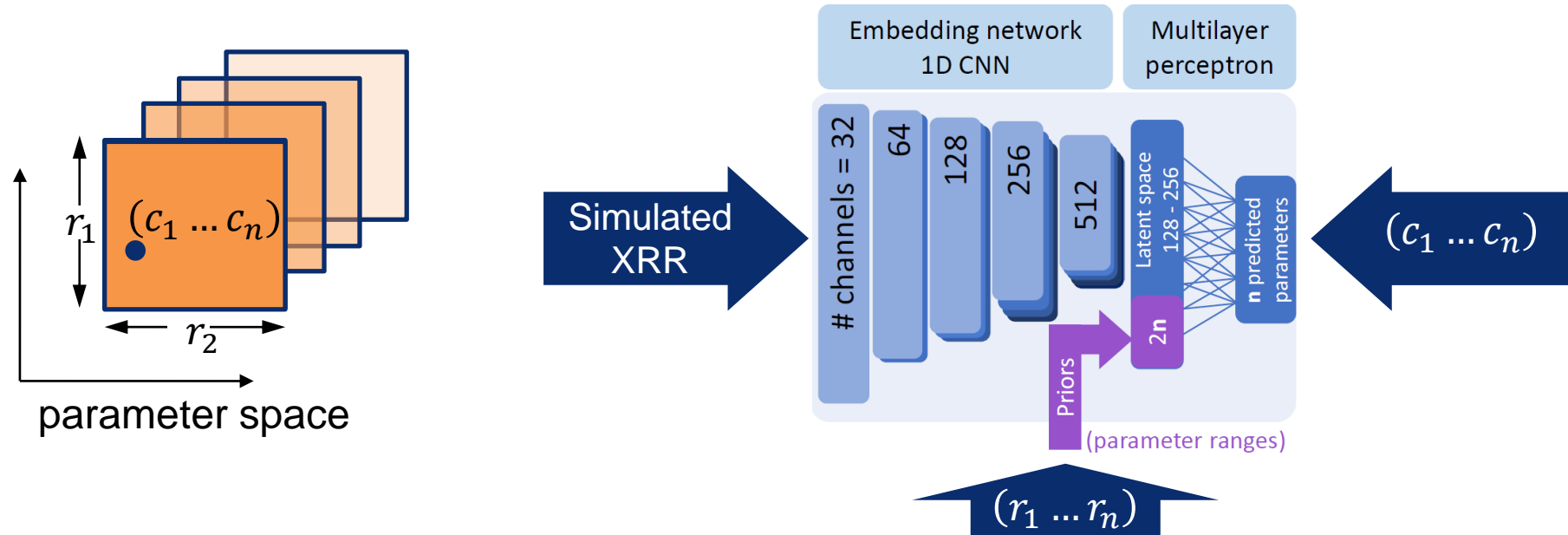
- Attempting to train a neural network as a point estimator over the domain containing the non-uniqueness leads to incorrect predictions corresponding

# Reflectorch: Including prior knowledge



- How to tackle ill-posed inverse problems by taking advantage of the *a priori* knowledge of experimentalists?

During Training:



Key aspects:

- Think of the training process as simultaneously learning on all possible subdomains (or a subset of subdomains) of the full parameter space

• [github.com/schreiber-lab/reflectorch](https://github.com/schreiber-lab/reflectorch)

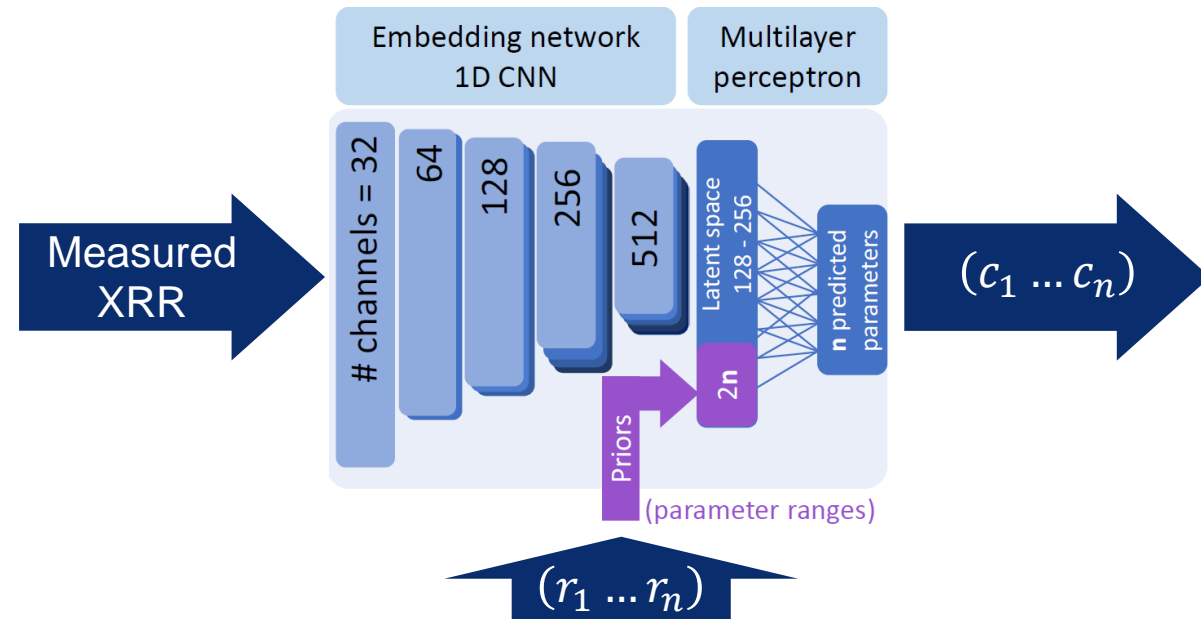
V. Munteanu, , V. Starostin, A. Greco, L. Pithan, A. Gerlach, A. Hinderhofer, S. Kowarik and F. Schreiber. J. Appl. Cryst. **57**, 2024, DOI 10.1107/S1600576724002115

# Reflectorch: Including prior knowledge



- How to tackle ill-posed inverse problems by taking advantage of the *a priori* knowledge of experimentalists?

At inference:



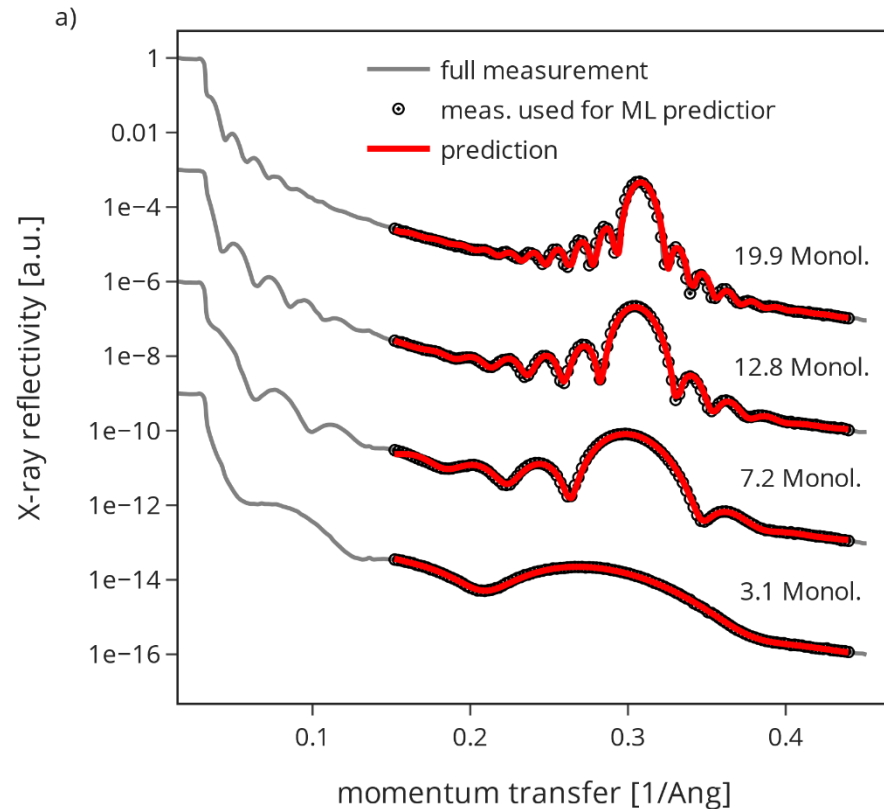
Key aspects:

- Think of the training process as simultaneously learning on all possible subdomains (or a subset of subdomains) of the full parameter space
- Combination of high speed of neural networks with the flexibility of conventional fitting procedures
- Embedding network produces latent embedding of XRR/NR data
- [github.com/schreiber-lab/reflectorch](https://github.com/schreiber-lab/reflectorch)

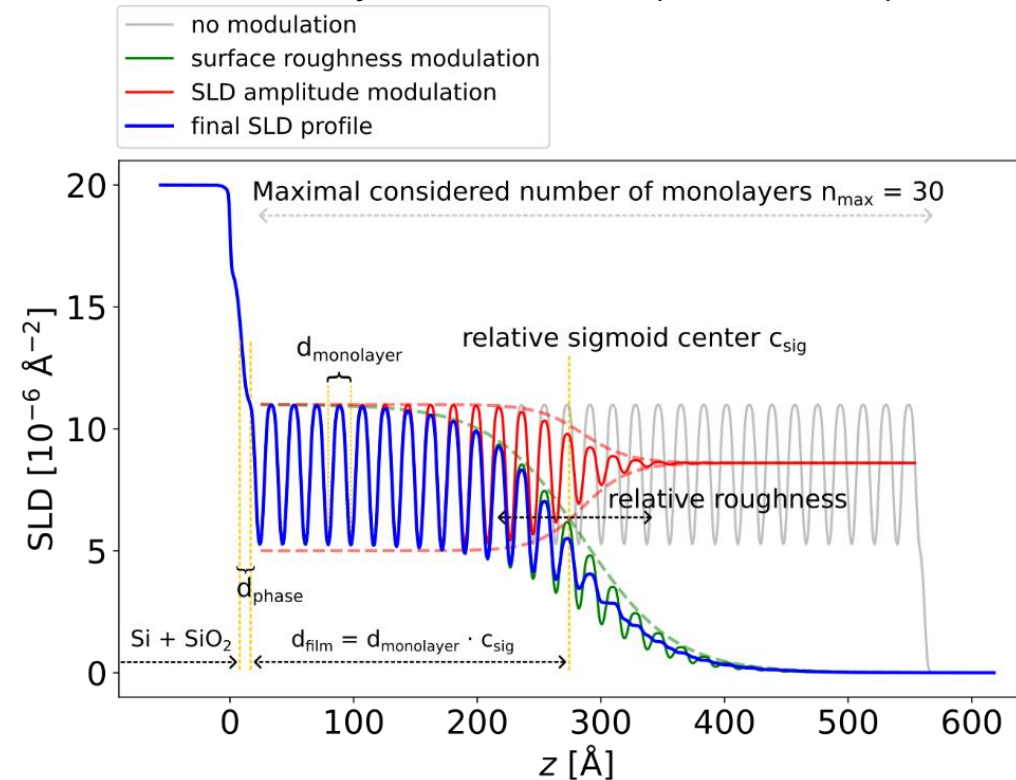
V. Munteanu, , V. Starostin, A. Greco, L. Pithan, A. Gerlach, A. Hinderhofer, S. Kowarik and F. Schreiber. J. Appl. Cryst. **57**, 2024, DOI 10.1107/S1600576724002115



## XRR data during growth (PTCDI-C8)



## Multilayer model for (PTCDI-C8)



- Enables physics informed parametrization
- Demonstrated to work for live feedback with more than 15 open parameters during film growth

L. Pithan et al, *Closing the loop: Autonomous experiments enabled by machine-learning-based online data analysis in synchrotron beamline environments*, J. Synchrotron Rad. **30** (2023) 1064

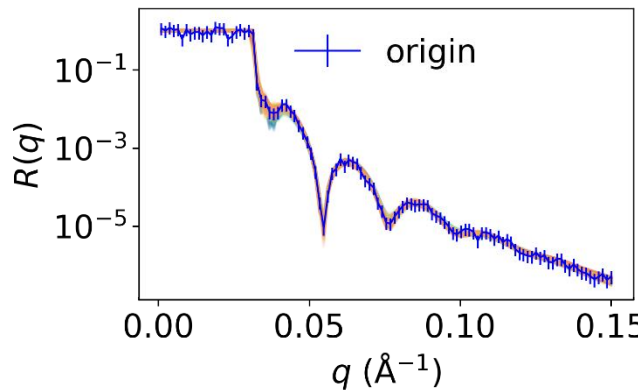
# Simulation-based inference (SBI) – general ML framework for Bayesian inference



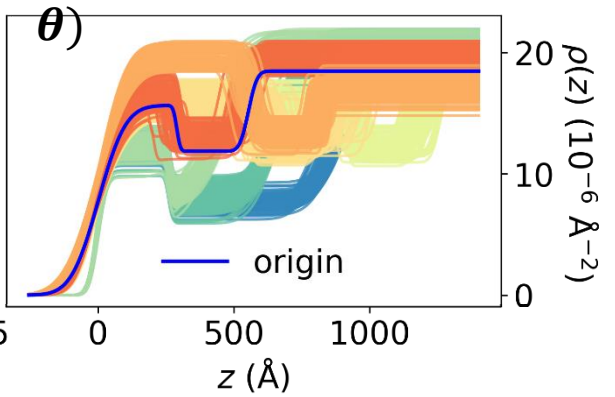
solutions (DBSCAN-clustered modes)



Reflectivity curves



SLD profiles (NPE, 10-dim)



Main Idea:

- Swap NN with e.g. Normalizing Flows
  - (take symmetries in the data into account)
- Get to probabilistic model

## Reliable

No missed solutions

*Dax et al. Phys. Rev. Lett., 2023, 130, 171403*

## Accurate

Result easily validated and **corrected**  
(Neural Importance Sampling)

*Müller et al., ACM Trans. Graph., 2019, 38, 1*

## Fast

Analysis performed in seconds

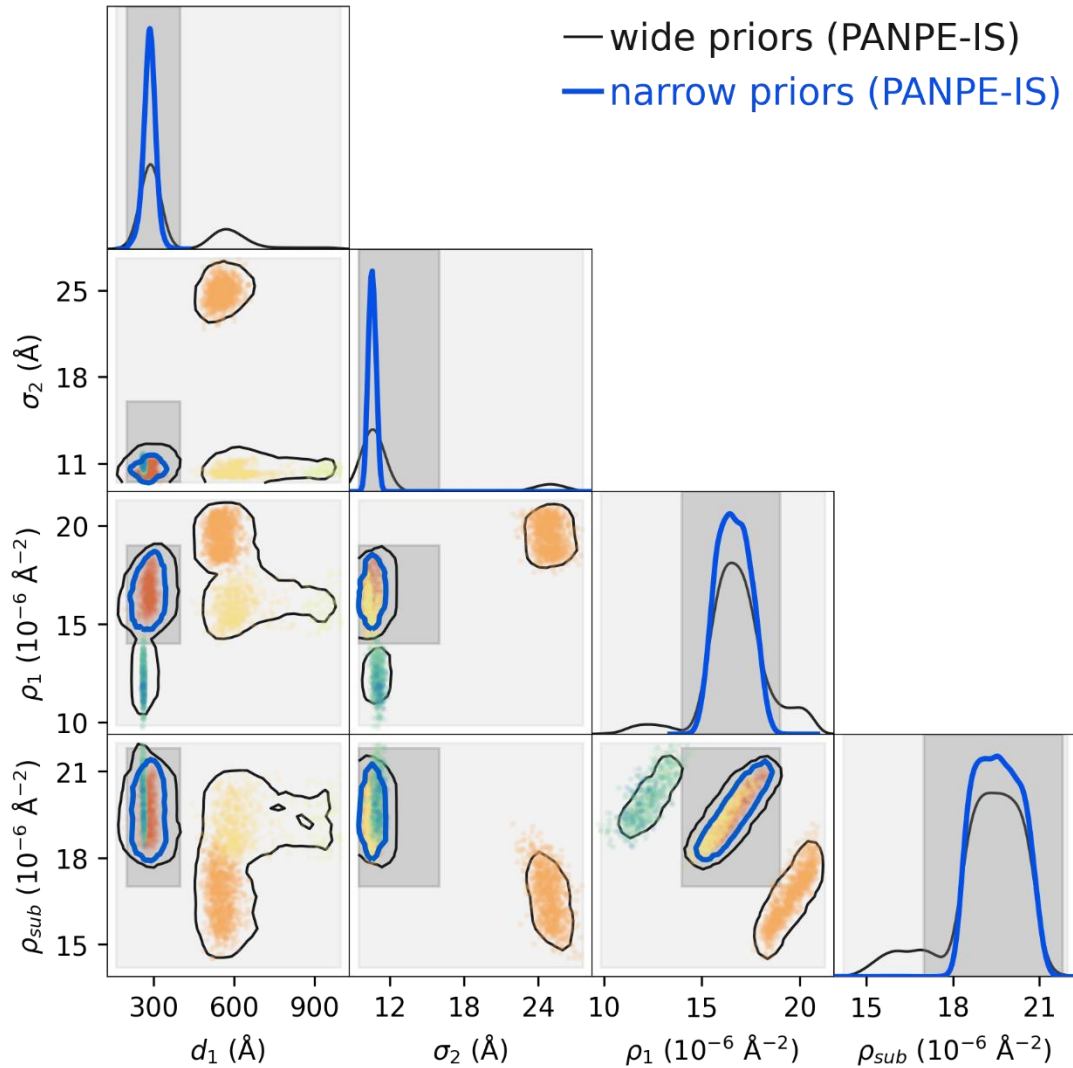
*Fast PyTorch simulator developed*

## Flexible

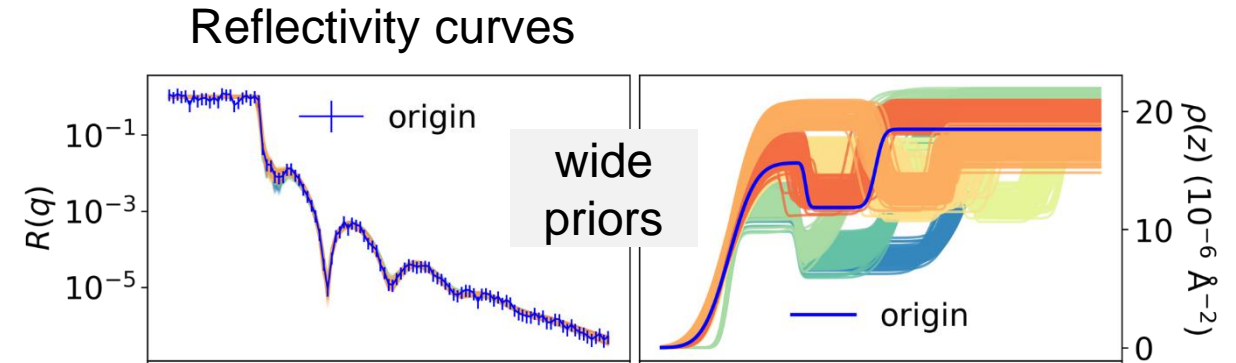
Prior-Amortized Neural Posterior  
Estimation (PANPE) approach  
enables incorporation of prior  
information

*Starostin et al., 2024*

# Incorporating dynamic prior information into SBI



solutions (DBSCAN-clustered modes)



# Vladimir Starostin

Roles **ML Research Scientist**

Photo

E-mail [vladimir.starostin@uni-tuebingen.de](mailto:vladimir.starostin@uni-tuebingen.de)



arXiv > physics > arXiv:2407.18648

Physics > Applied Physics

[Submitted on 26 Jul 2024]

## Fast and Reliable Probabilistic Reflectometry Inversion with Prior-Amortized Neural Posterior Estimation

Vladimir Starostin, Maximilian Dax, Alexander Gerlach, Alexander Hinderhofer, Álvaro Tejero-Cantero, Frank Schreiber

Subjects: **Applied Physics (physics.app-ph)**; Soft Condensed Matter (cond-mat.soft); Machine Learning (cs.LG); Machine Learning (stat.ML)

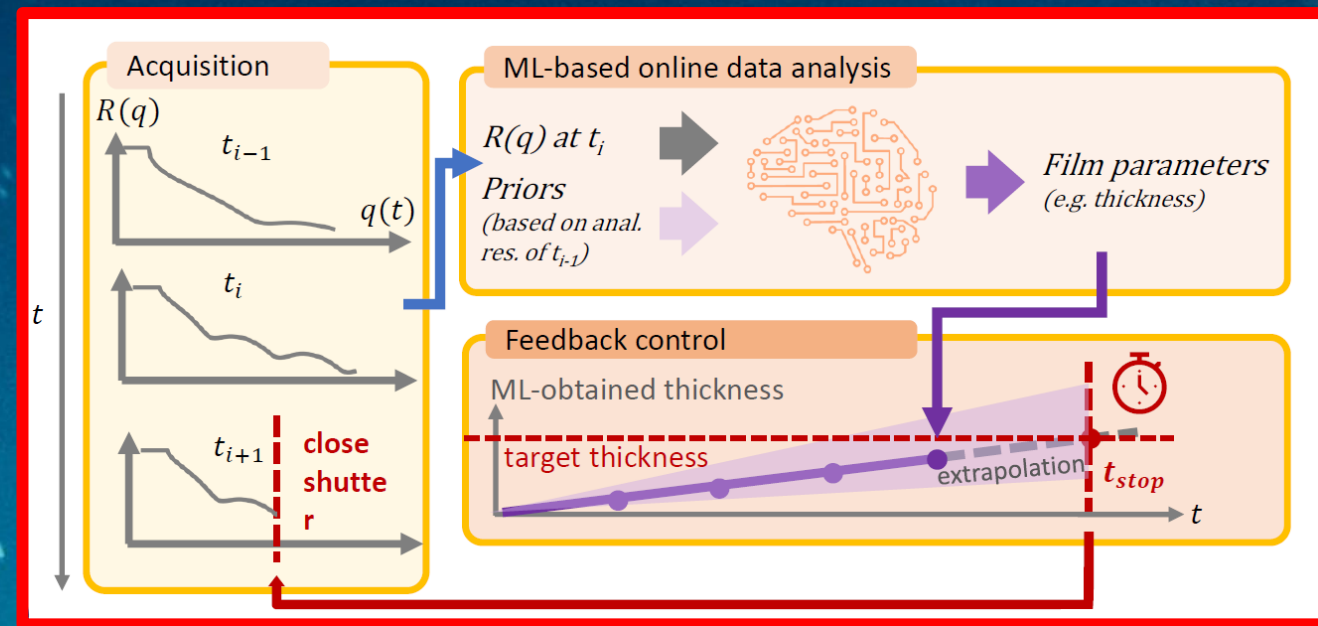
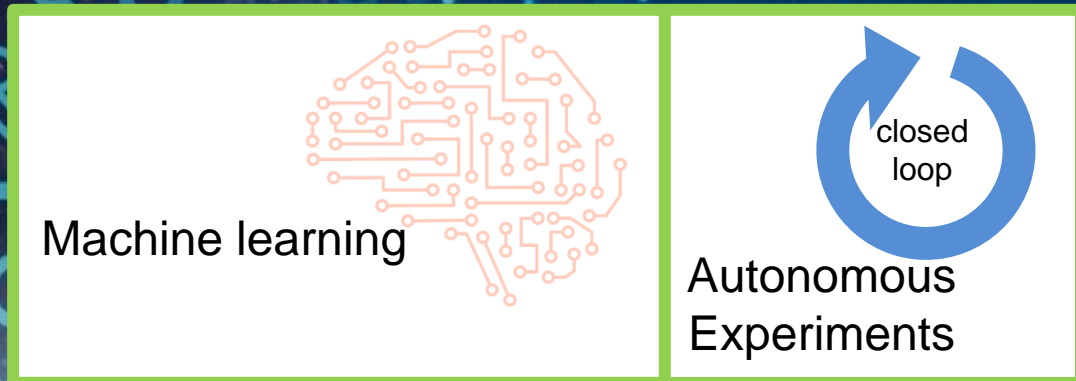
Cite as: [arXiv:2407.18648](https://arxiv.org/abs/2407.18648) [physics.app-ph]

(or [arXiv:2407.18648v1](https://arxiv.org/abs/2407.18648v1) [physics.app-ph] for this version)

<https://doi.org/10.48550/arXiv.2407.18648> 

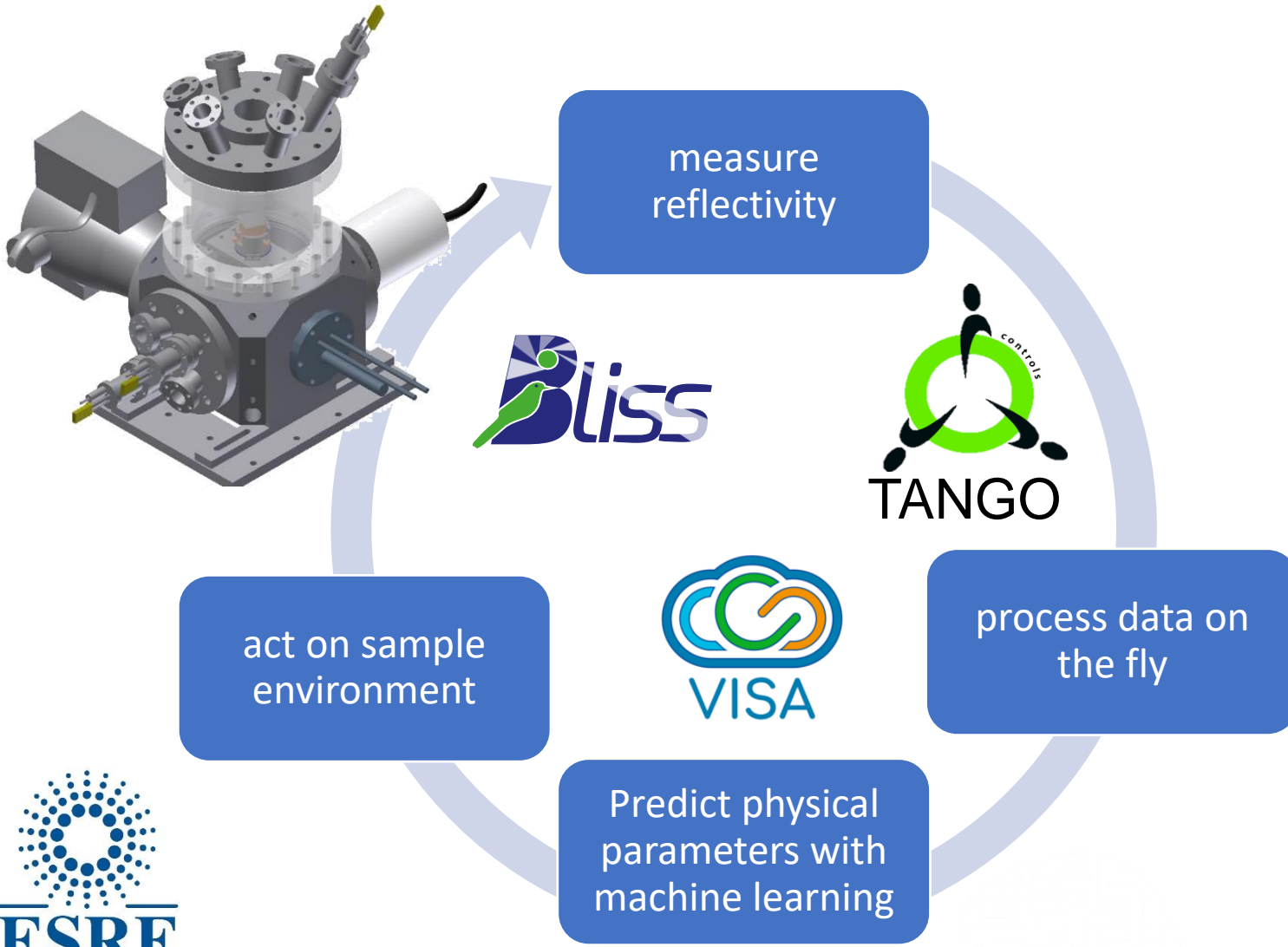
submitted to ScienceAdvances



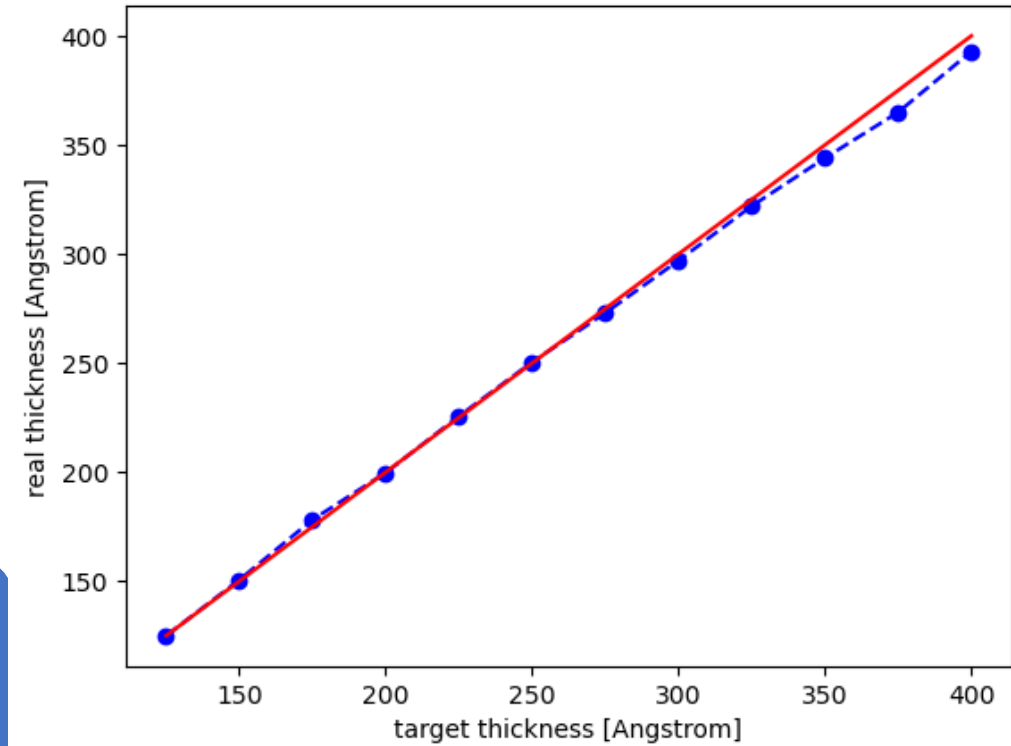


DAPHNE  
4NFDI

# A simple autonomous experiment



AI - controlled thin film deposition



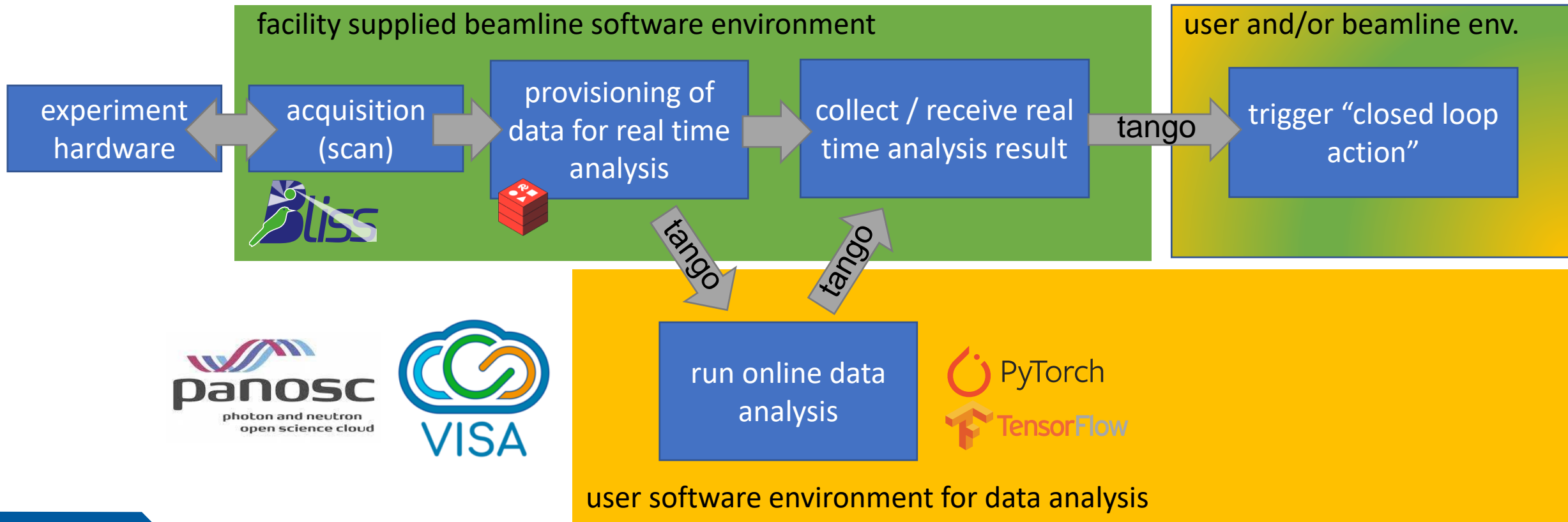
L. Pithan et al, J. Synchrotron Rad. **30** (2023) 1064  
J.-F. Perrin, ESRF Highlights 2022, 158-159 (2022).  
<https://www.tango-controls.org>,  
<https://bliss.gitlab-pages.esrf.fr/bliss>



# Software environments



- No need for user software to be installed in the beamline environment





## Outlook: ML integration into loop beamline operation

- What infrastructure should facilities provide to enable visiting users to systematically perform autonomous experiments ?
- How transferable can these solutions between facilities in order to be transparent for the user?

### PETRA IV.

Which control system to choose?

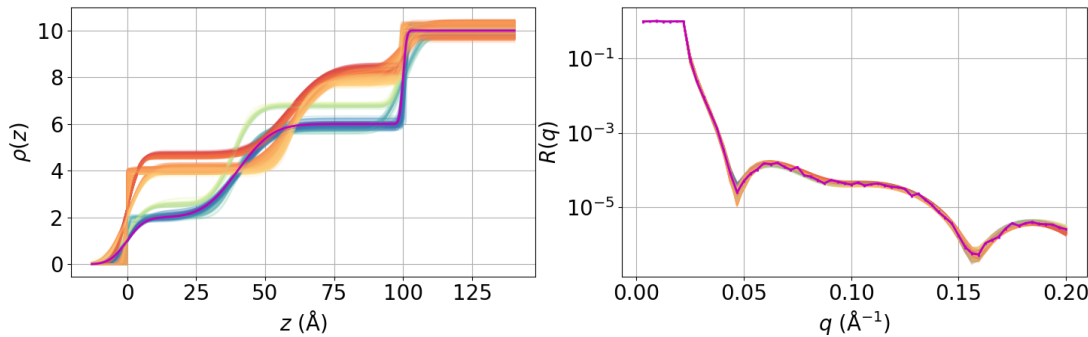


**DIGITAL @ LEAPS**  
**Fully Automated Beamline**

Please get in touch with me in case you'd like to be involved!

# Summary

- Neural networks for “fitting” XRR data
  - Multilayer Percepton (ML-Reflect package)
  - Incorporation of prior knowledge (Relectorch package)
  - Prior-Amortized Neural Posterior Estimation (PANPE)
- Closed loop feedback & beamline integration



Main references:

[github.com/schreiber-lab](https://github.com/schreiber-lab)

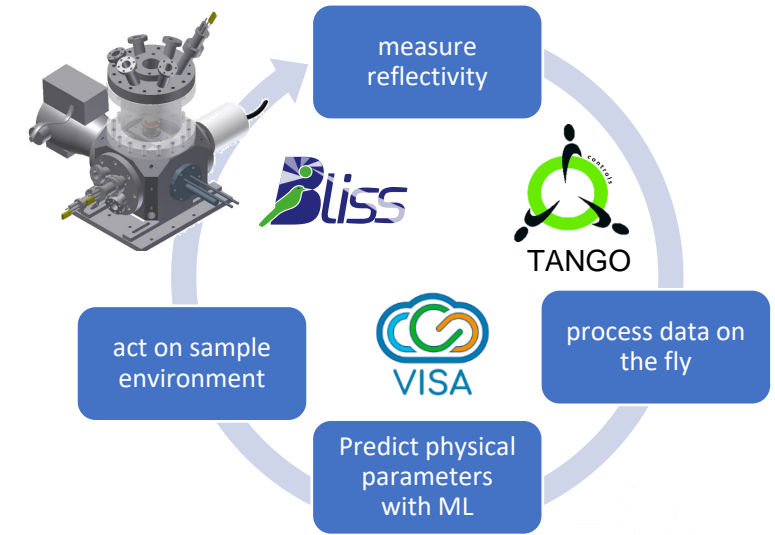
L. Pithan et al, *J. Synchrotron Rad.* 30 (2023) 1064

A. Greco et al., *J. Appl. Cryst.* 55, 362 (2022)

A. Hinderhofer et al., *J. Appl. Cryst.* 56 (2023)

V. Munteanu et al., *J. Appl. Cryst.* 57 (2024)

V. Starostin et al., 2024, 10.48550/arXiv.2407.18648



zenodo

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Communities

May 27, 2022

Dataset Open Access

Reflectometry curves (XRR and NR) and corresponding fits for machine learning

Pithan, Linus; Greco, Alessandro; Hinderhofer, Alexander; Gerlach, Alexander; Kowarik, Stefan; Rußegger, Nadine; Dax, Ingrid; Schreiber, Frank



**Labelled reflectometry data**

L.Pithan et al. 2022 <https://doi.org/10.5281/zenodo.6497438>



# Different approaches to inverse problem with ML

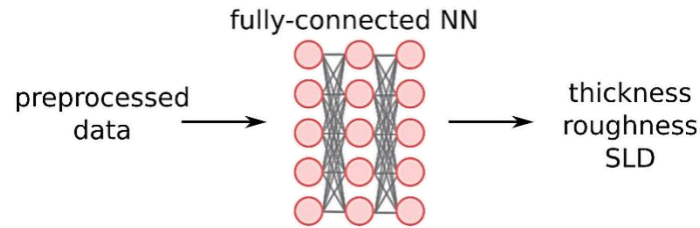


In general, inverse problem in reflectometry is ill-posed due to *the phase problem* → *possible multimodal solutions*

**Point estimators.** To avoid ambiguity, **the task should be narrowed down to specific cases** (e.g., silicon + silicon oxide + organic layer)

**Probability density estimators.** Resolves the ambiguity issue

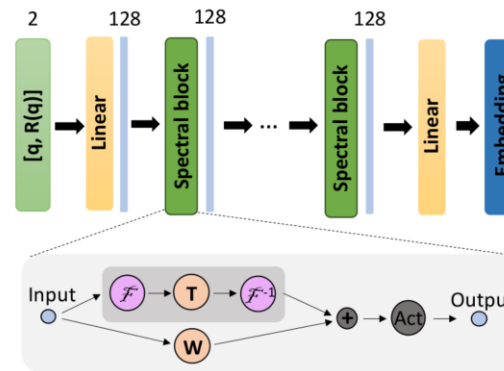
## Regression via NNs (MLP, CNN, ...)



Greco et al. J. Appl. Cryst. 2022, 55, 362  
Greco et al. Mach. Learn.: Sci. Technol. 2021, 2, 045003  
Greco et al. J. Appl. Cryst. 2019, 52, 1342

- Simple implementation
- Fast inference
- Fails on multimodal cases
- Does not account for parameter distribution
- Does not provide error bars / uncertainty estimation
- Likely that retraining the ML-model is needed for different use cases

## Fourier Neural Operator (FNO)

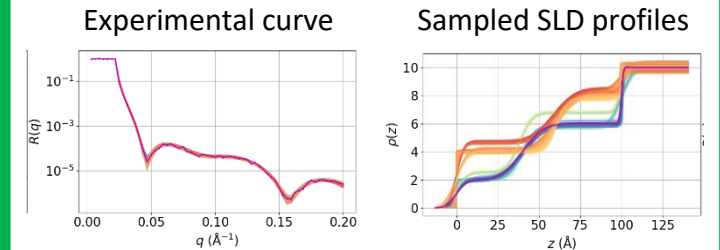


V. Munteanu et al., J. Appl. Cryst. 2024, 57,  
DOI: 10.1107/S1600576724002115

- Discretization-invariant learning

## Normalizing Flows

neural posterior estimation



Sample profiles via conditional inverse Normalizing Flows transformation

Starostin et al., 2024

- Accelerated Bayesian analysis
- Resolves ambiguity problem
- Provides error bars
- No retraining required
- More difficult to implement

# Generation 1 (2019-2022): MLReflect



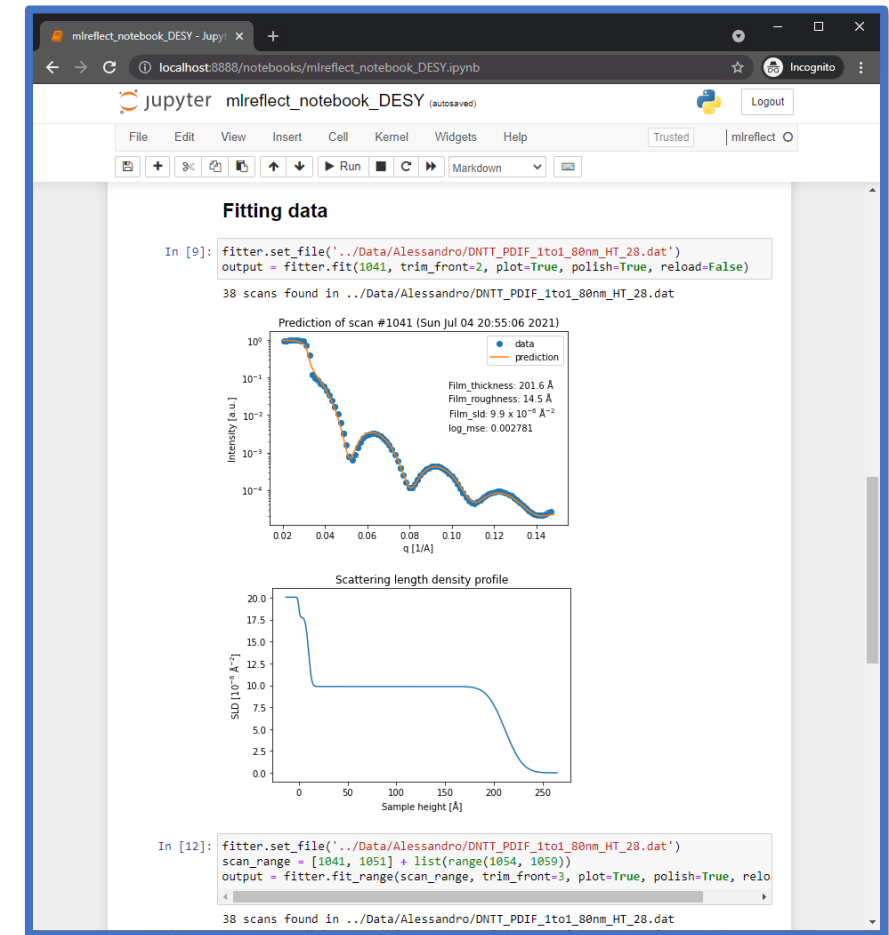
## Python package *MLReflect*

### BMBF project in collaboration with DESY

- Available on GitHub / PyPI
- Online documentation available on Read the Docs
- Can be used with Jupyter notebooks as GUI
- Installed at DESY, PETRA III, P08

### Remaining challenges

- Parameter ranges are defined during training stage.
- Discretization to be defined during training stage.
- Does not work reliable for complex multilayer structures
- No estimation of error bars



[github.com/schreiber-lab/mlreflect](https://github.com/schreiber-lab/mlreflect)

Greco et al., *J. Appl. Cryst.* **55**, 362 (2022)

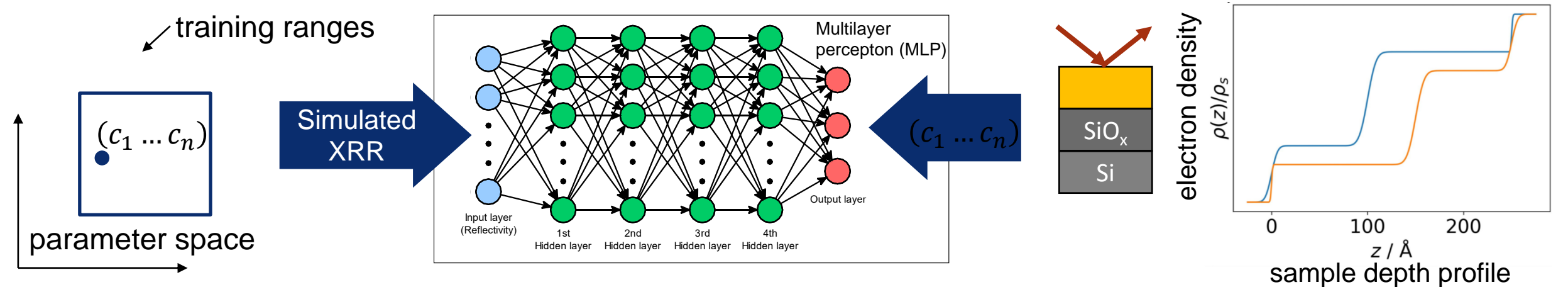


# Generation 2: Including prior knowledge



- How to tackle ill-posed inverse problems by taking advantage of the *a priori* knowledge of experimentalists?

“Standard” / classical approach to train the ML model:



Classical approach for model training:

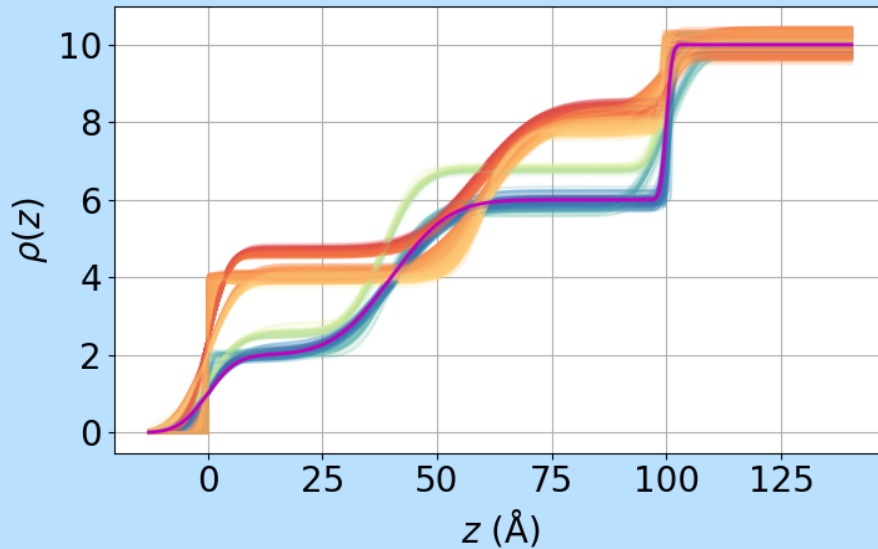
- Sample can only be trained for “small” parameter space, where a model can be trained
- simulate XRR + noise can be assumed!
- gradient descent in MLP
- consequence: make sure that e.g. only the orange curve falls in training ranges
- Training of “general” model not possible
- No option for the experimentalist to “guide” the model

V. Munteanu et al., J. Appl. Cryst. (2024, accepted), 57,  
DOI: 10.1107/S1600576724002115

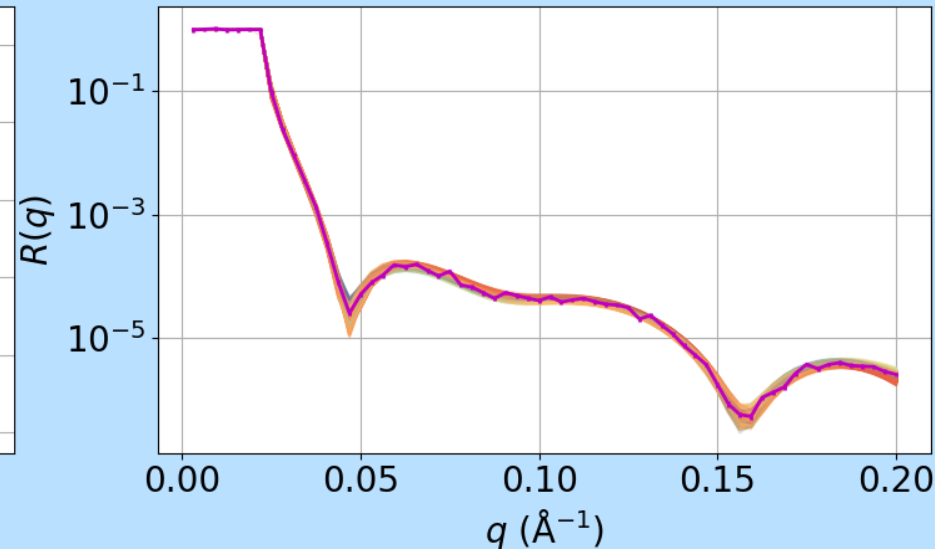
# Underdetermined inverse problems



- forward process maps parameters of physical system to an observable signal
- inverse problem describes the retrieval of physical parameters from a (possibly noise-corrupted) measurement of the signal
  - **one-to-one mapping**: training of neural network straightforward to approximate inverse function
  - **many-to-one** mapping (forward process): leads to an underdetermined, ill-posed inverse problem with corresponding **one-to-many** inverse mapping that cannot be approximated via regression.



depth in sample



scattering vector

V. Munteanu et al, J. Appl. Cryst. **accepted, (2024)**

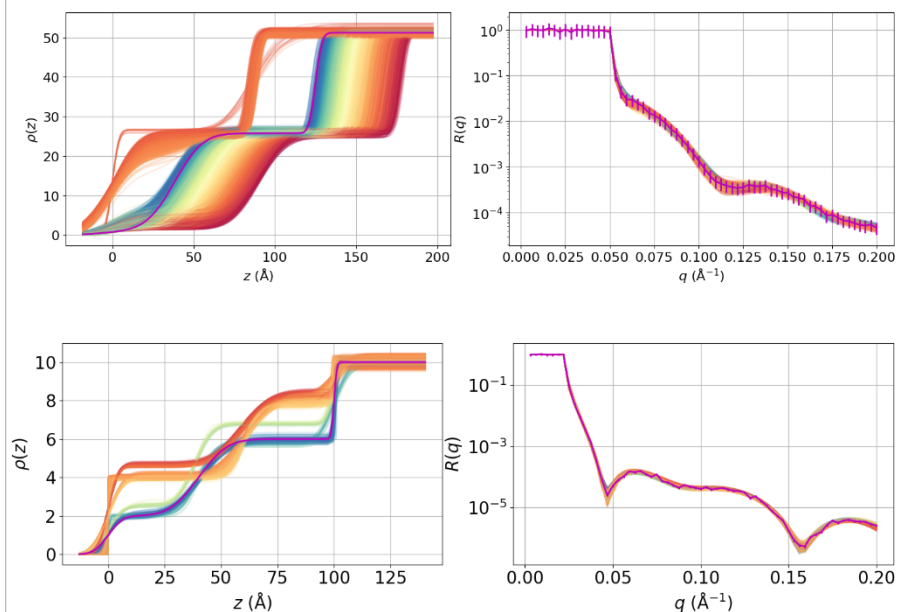
V. Starostin et. al , **in prep.**

# Confirmed hypothesis about high levels of ambiguity



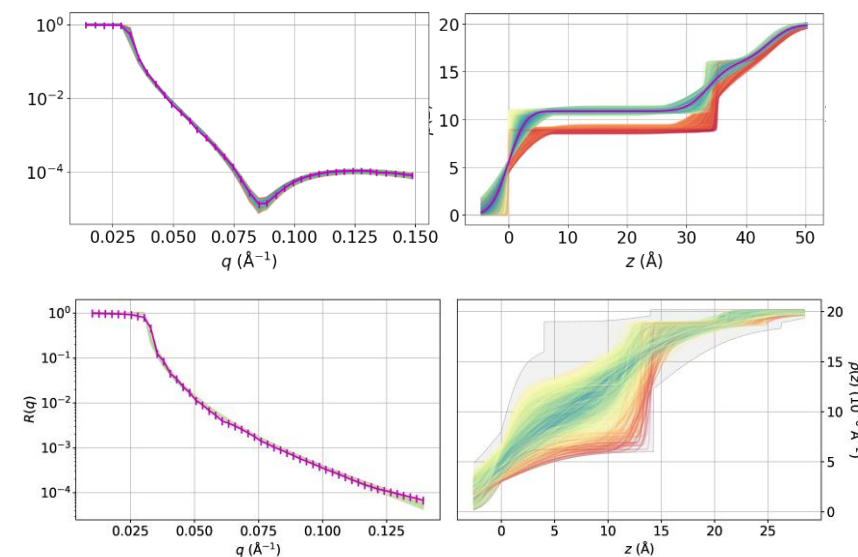
## Simulated data from two-layered structures

SLD profiles (PANPE) Reflectivity curves



## Experimental data (one-layer) used for benchmarking ML

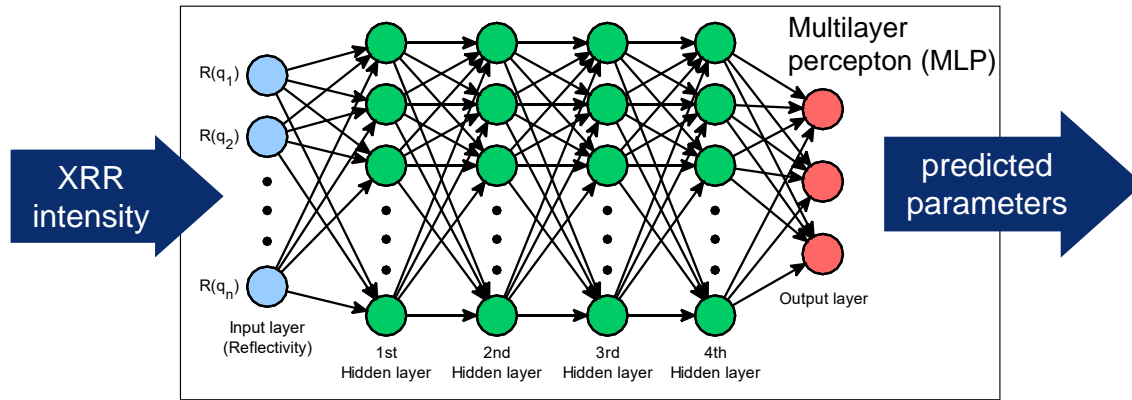
Reflectivity curves SLD profiles (PANPE)



# Gen 2.2: Discretization-invariant learning



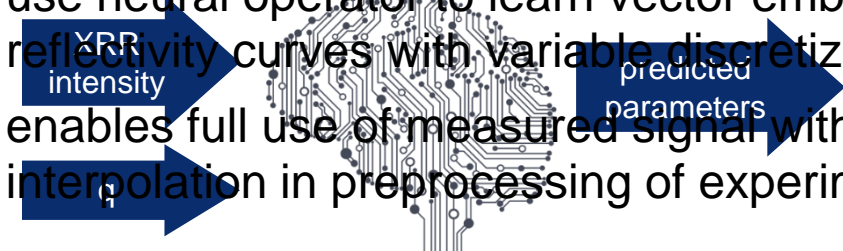
- in traditional approach: Only XRR curves as input, q-base is fixed



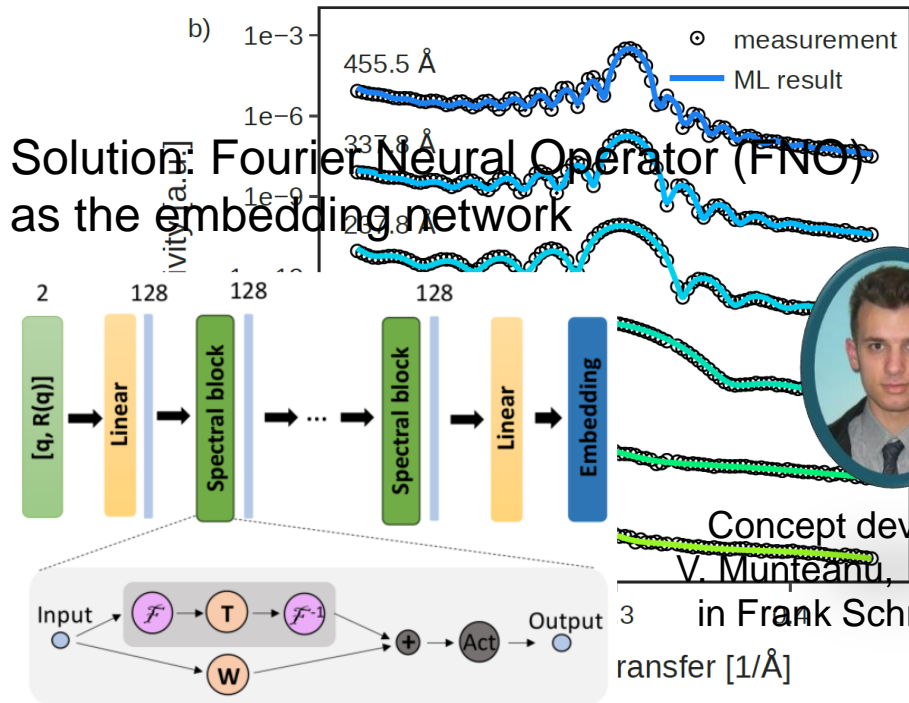
Problem:

- Neural networks can only learn mappings between finite-dimensional vector spaces.
- Multilayer perceptron requires a fixed discretization (range and resolution) of the input

- How to become more flexible in q-discretization?
- use neural operator to learn vector embedding for reflectivity curves with variable discretizations
- enables full use of measured signal without relying on interpolation in preprocessing of experimental data



- Solution: Fourier Neural Operator (FNO) as the embedding network

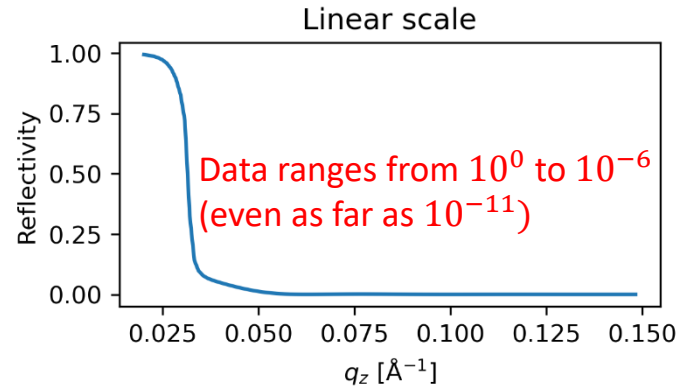


Concept developed by  
V. Munteanu, PhD student  
in Frank Schreiber's lab  
transfer [ $1/\text{\AA}$ ]

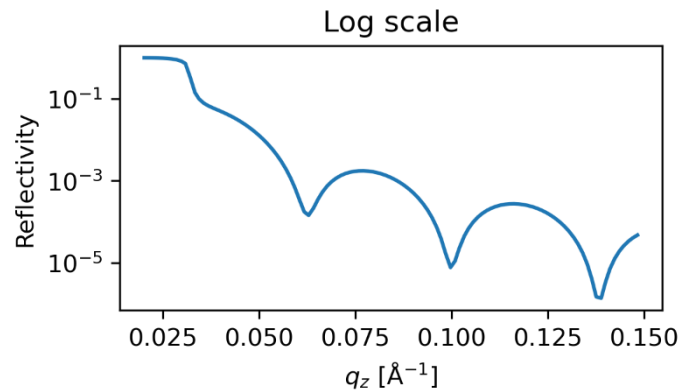
V. Munteanu et al., J. Appl. Cryst. (2024, accepted), 57,  
DOI: 10.1107/S1600576724002115



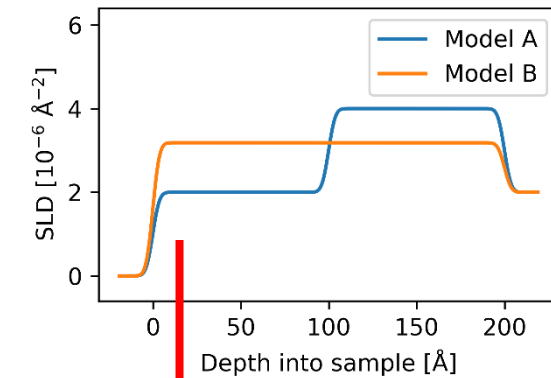
## 1. High dynamic range



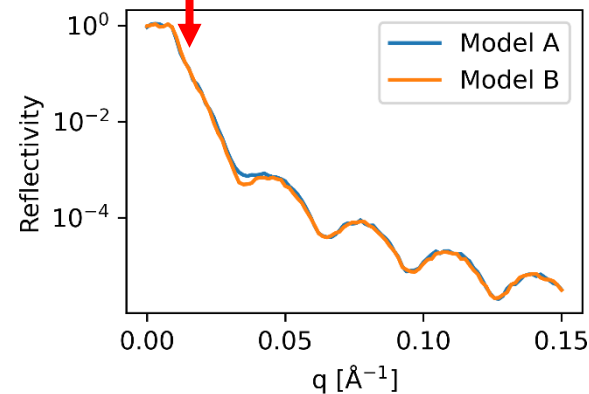
Log scale can help, but inputs are still not equally distributed



## 2. Phase problem/ambiguity

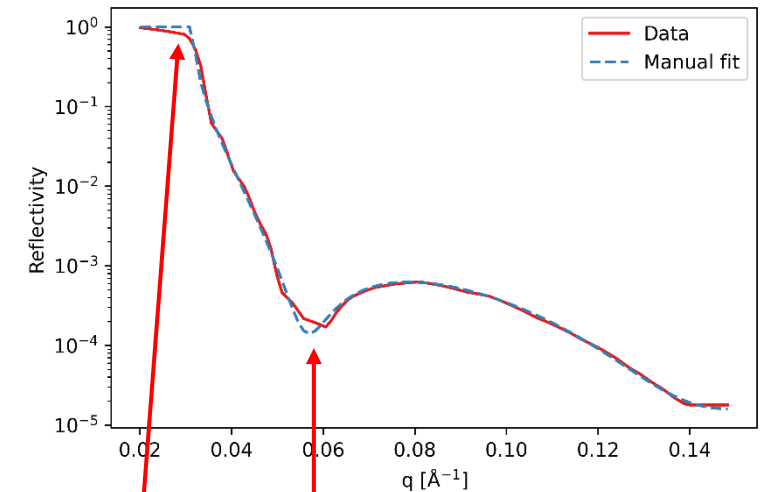


Different samples create the same reflectivity signal!



## 3. Experimental artifacts

The neural network is trained with simulated data, but meant to be used with experimental data!



Experiment and theory do not follow the same distribution!

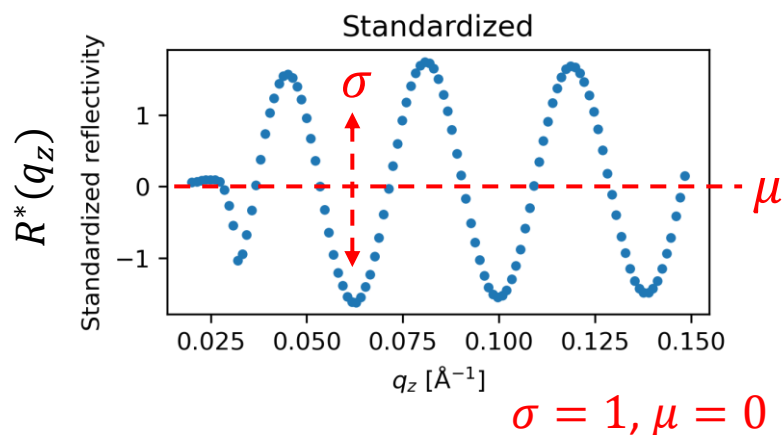


## 1. High dynamic range

Standardize input

$$R^*(q_z) = \frac{R(q_z) - \bar{R}(q_z)}{\hat{R}(q_z)}$$

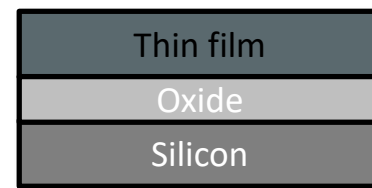
- $\bar{R}(q_z)$ : mean
- $\hat{R}(q_z)$ : standard deviation
- derived from training set with artificial noise



## 2. Phase problem/ambiguity

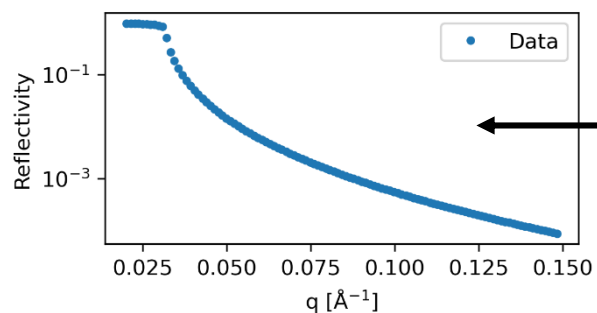
Reduce solution space (add “priors”)

E.g., 3 thin film parameters with a certain range



- ← varied Thickness 20 – 1000 Å
- ← fixed Roughness 0 – 40 Å
- ← fixed SLD 1 – 14 10<sup>-6</sup>Å<sup>-2</sup>

Remove “featureless” curves



Exclude from training:

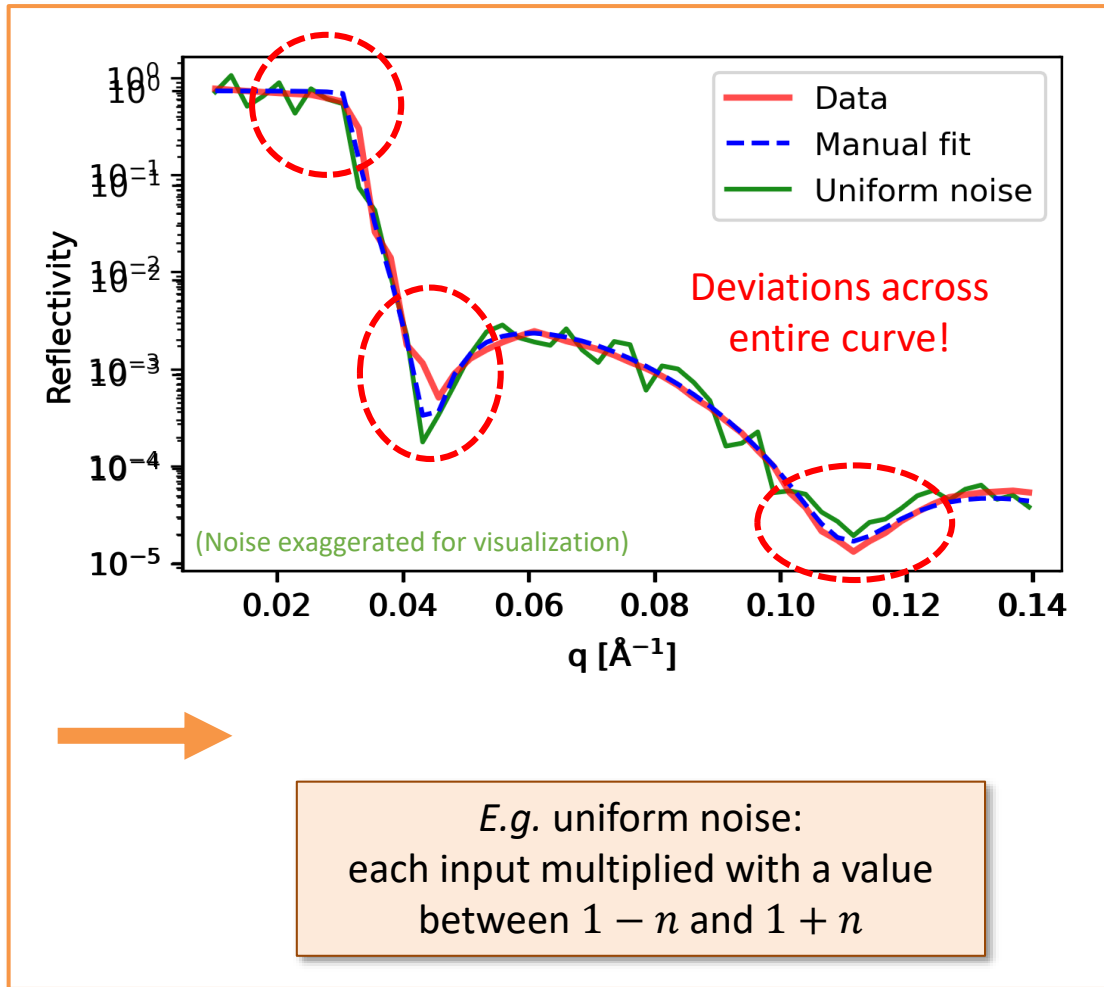
- Low thickness: < 20 Å
- Low contrast: < 10<sup>-6</sup> Å<sup>-2</sup>
- High roughness: > 40 Å

Greco et al. *Mach. Learn.: Sci. Technol.*, 2021, 2, 045003

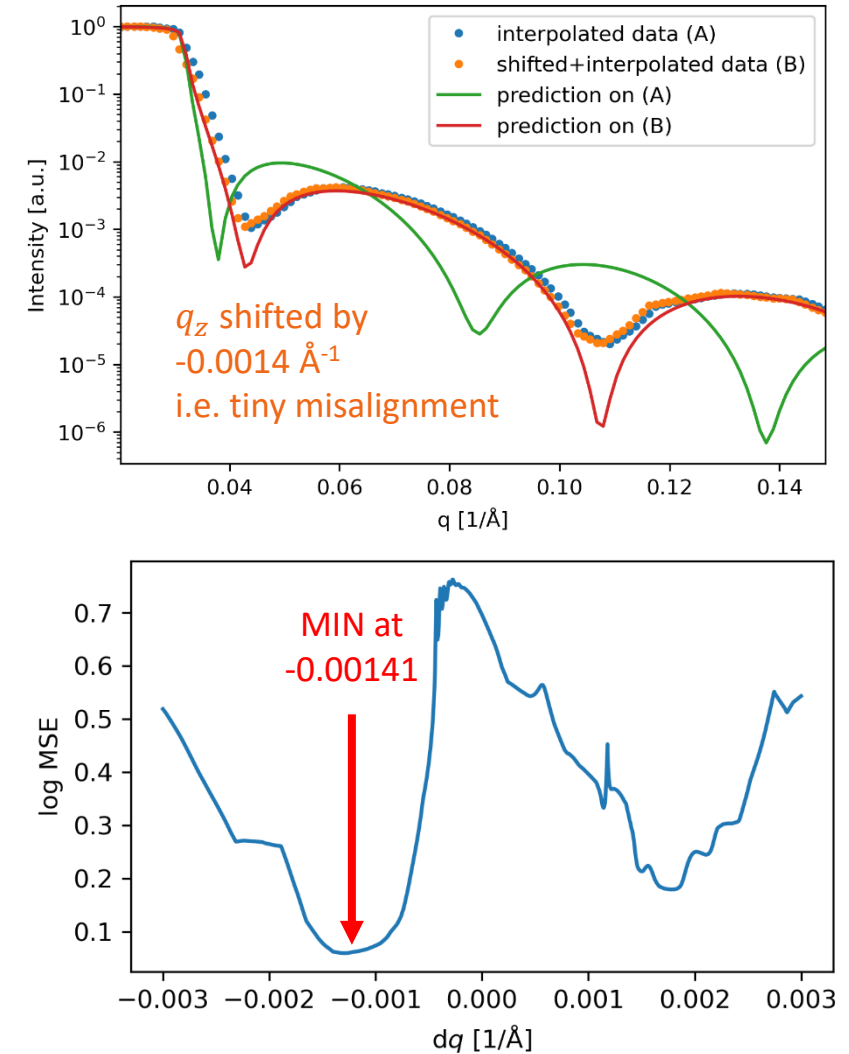




## 3. Experimental artifacts (noise, misalignment, ...)



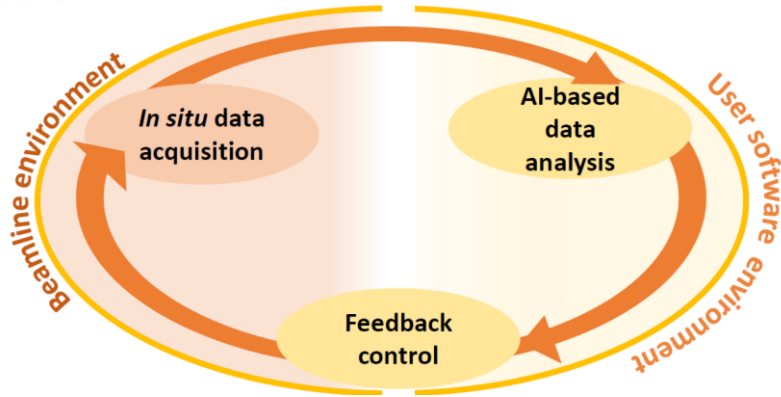
## PEN on Si/SiO<sub>x</sub>



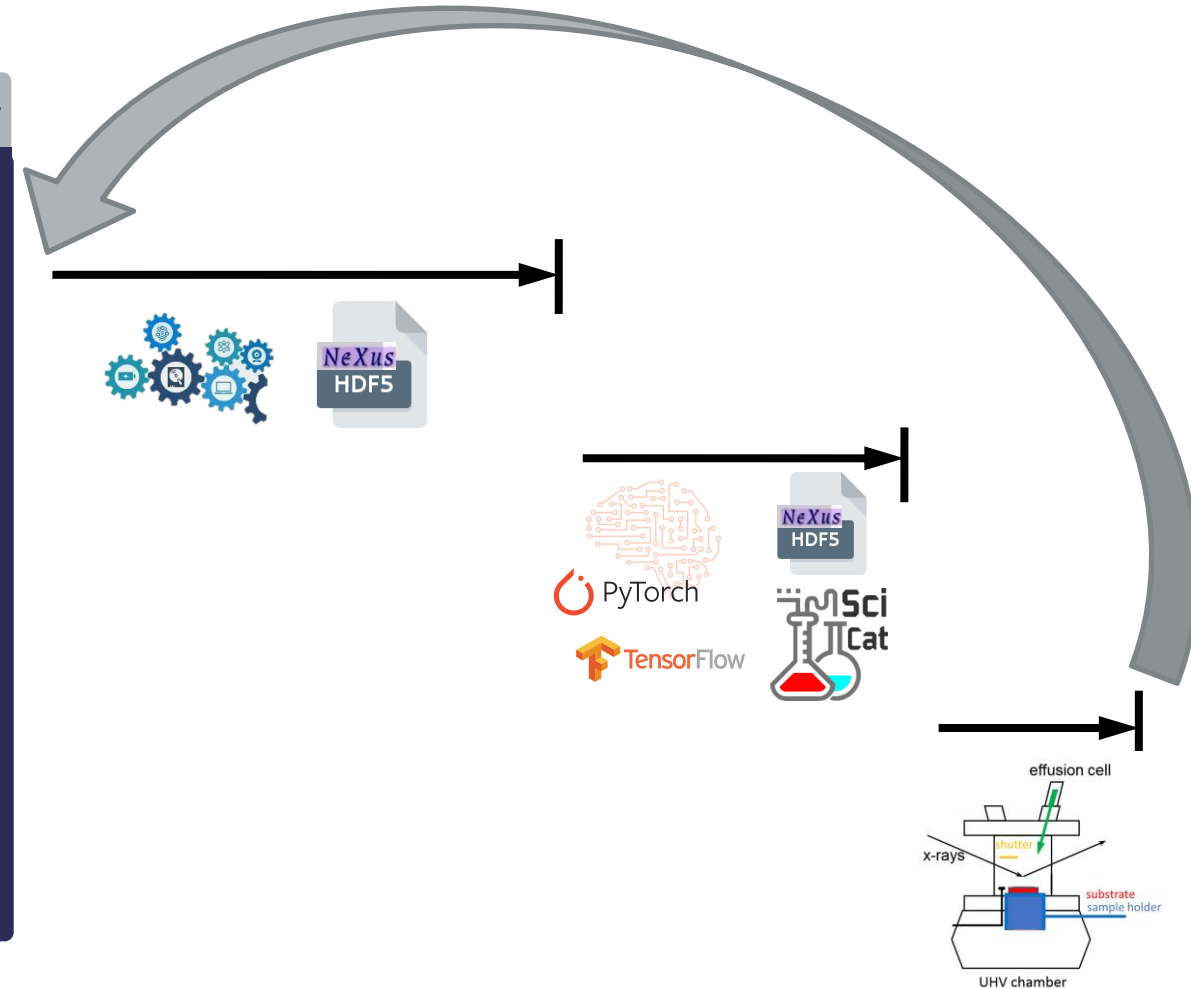
# Feedback scheme



(a) Synchronous loop



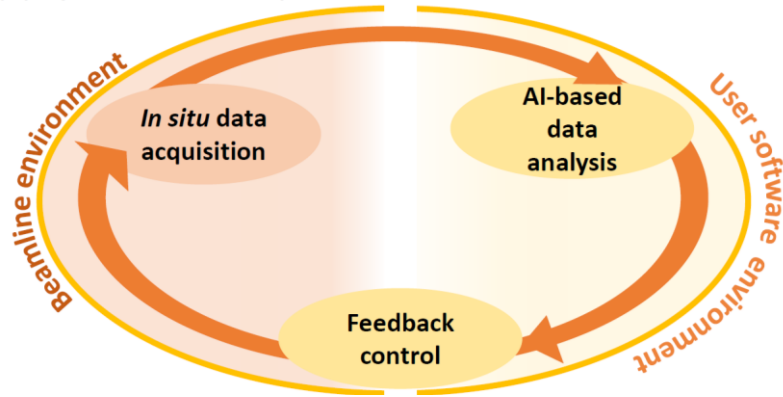
```
> while(True):  
  s = a2scan(...)  
  
  d = predict(s)  
  
  if d > 50:  
    stop_growth()  
    break
```



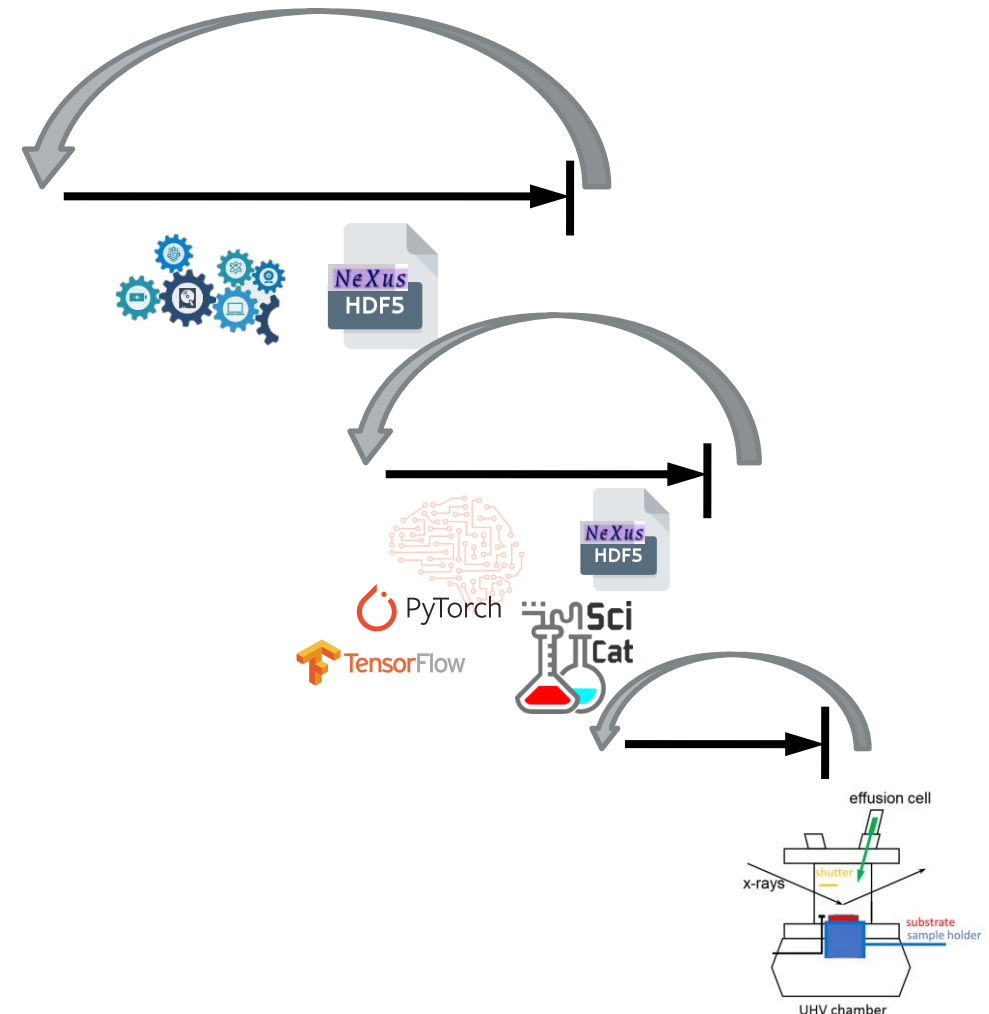
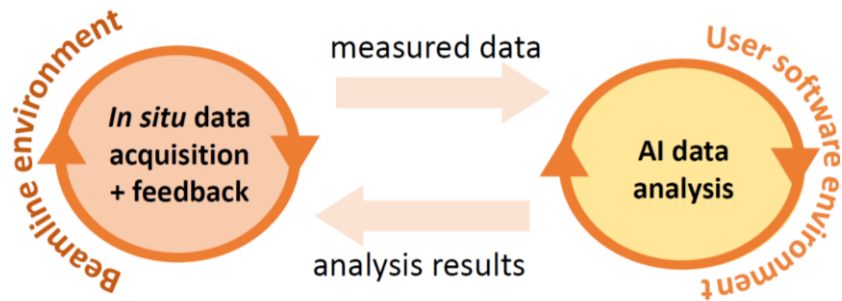
# Feedback scheme



(a) Synchronous loop



(b) Asynchronous loops



# Public XRR dataset



May 27, 2022

Dataset Open Access

## Reflectometry curves (XRR and NR) and corresponding fits for machine learning

Pithan, Linus; Greco, Alessandro; Hinderhofer, Alexander; Gerlach, Alexander; Kowarik, Stefan; Rußegger, Nadine; Dax, Ingrid; Schreiber, Frank

### Public reflectometry data collection

- about 250 experimental XRR profiles
- labelled data: sample parameters & classical fits are published together with measurements
- indented to grow
  - call for contributing datasets
  - plans for dedicated infrastructure

```
In [1]: #prepare jupyter notebook for plots shown below
%run prepare_plot.py

#imports
from silx.io.dictdump import nxdodict #read NeXus hdf5 to python dict
import numpy as np
import pandas as pd
from IPython.display import display

#use same q_range as during fitting
q_fit = np.linspace(0.02,0.15,130,endpoint=False)

#produce plots
for key, ds in nxdodict("xrr_dataset.h5").items():
    if "@ not in key: #skip nexus attributes

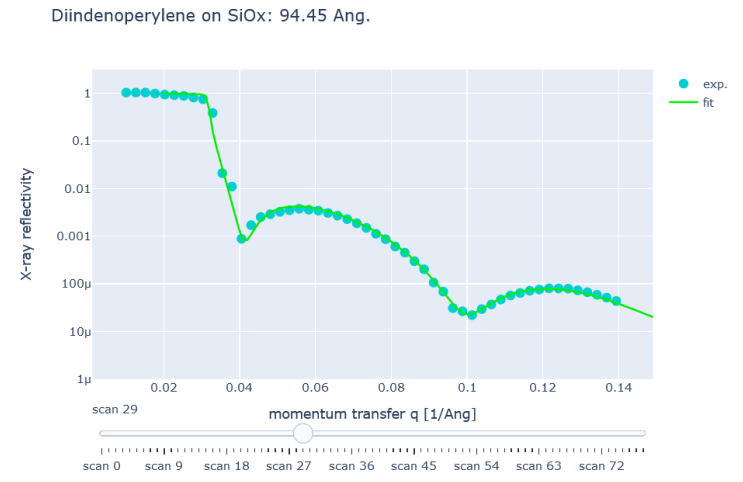
        print("Dataset: ",key)
        print("Experimentalists: ",ds["metadata"].pop("Experimentalists","?"))
        ds["metadata"].pop("@NX_class","")
        display(pd.DataFrame.from_dict({"Dataset":key,**ds["metadata"]}))

        fig = prepare_figure(ds,q_fit,str(ds["metadata"]["Layer_material"])+ " on SiOx")
        fig.show()
```

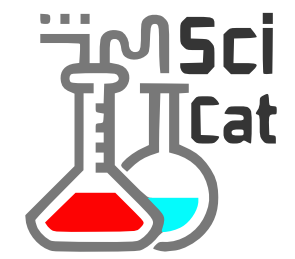
NeXus

Dataset: DIP\_1  
Experimentalists: ['Kowarik, Stefan']

Dataset	Layer_CAS	Layer_formula	Layer_material	Substrate_temperature	Substrate_temperature@unit	instrument	q_max
0	DIP_1	188-94-3	C32H16	Diindenoperylene	303	K	ESRF, ID10b



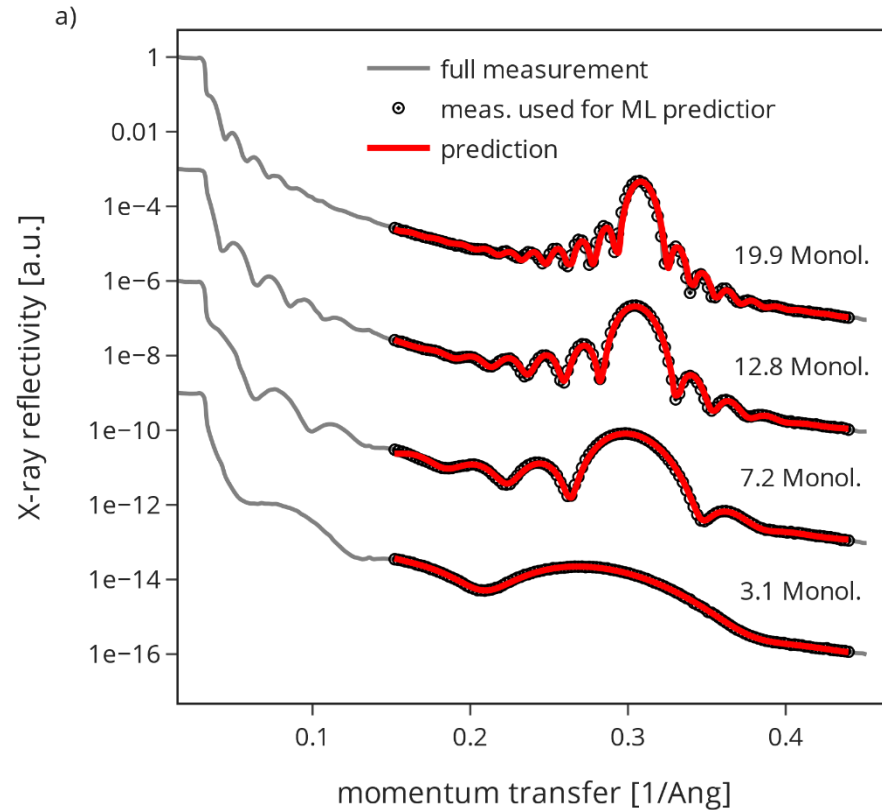
Foreseen collaboration:



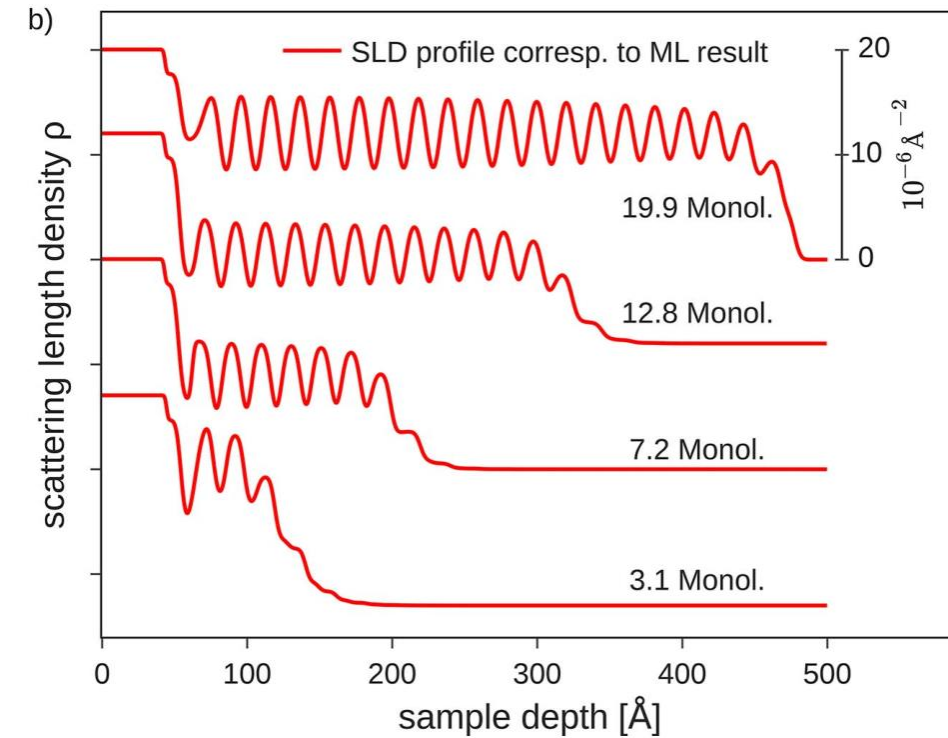
# Multilayers and 15+ parameters



## XRR data during growth (PTCDI-C8)



## SLD profiles for (PTCDI-C8)



L. Pithan et al, *Closing the loop: Autonomous experiments enabled by machine-learning-based online data analysis in synchrotron beamline environments*, J. Synchrotron Rad. **30** (2023) 1064